

Mathematical modeling of white adipocyte exocytosis predicts adiponectin secretion and quantifies the rates of vesicle exo- and endocytosis.

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Abstract

Adiponectin is a hormone secreted from white adipocytes and takes part in the regulation of several metabolic processes. Although the pathophysiological importance of adiponectin has been thoroughly investigated, the mechanisms controlling its release are only partly understood.

We have recently shown that adiponectin is secreted via regulated exocytosis of adiponectin-containing vesicles, that adiponectin exocytosis is stimulated by cAMP-dependent mechanisms and that Ca^{2+} and ATP augments the cAMP-triggered secretion. However, much remains to be discovered regarding the molecular and cellular regulation of adiponectin release.

Here we have used mathematical modeling to extract detailed information contained within our previously obtained high-resolution patch-clamp time-resolved capacitance recordings to produce the first model of adiponectin exocytosis/secretion that combines all mechanistic knowledge deduced from electrophysiological experimental series. This model demonstrates that our previous understanding of the role of intracellular ATP in the control of adiponectin exocytosis needs to be revised to include an additional ATP-dependent step. Validation of the model by introduction of data of secreted adiponectin, yielded a very close resemblance between the simulations and experimental results. Moreover, we could show that Ca^{2+} -dependent adiponectin endocytosis contributes to the measured capacitance signal and we were able to predict the contribution of endocytosis to the measured exocytotic rate under different experimental conditions. In conclusion, using mathematical modeling of published and newly generated data, we have obtained estimates of adiponectin exo- and endocytosis rates and we have predicted adiponectin secretion. We believe that our model should

have multiple applications in the study of metabolic processes and hormonal control thereof.

Introduction

Adiponectin is a hormone exclusively secreted from white adipocytes with roles in regulation of glucose and lipid levels. Obesity and type 2 diabetes are associated with reduced circulating levels of adiponectin. Moreover, high adiponectin levels protect against development of type 2 diabetes (1). Albeit the pathophysiological relevance of adiponectin is clearly, the molecular regulation of its release is inadequately studied. Similarly to other hormones (2), adiponectin has been proposed to be released via regulated exocytosis (3-5). However, the molecular mechanisms controlling adiponectin vesicle release are not fully resolved. Our previous work has demonstrated that adiponectin is released from an intracellular pool of adiponectin-containing vesicles (6,7). However, unlike most peptide/protein hormones (2), exocytosis of adiponectin is triggered by cAMP and a combination of intracellular Ca^{2+} and ATP potentially augments the cAMP-stimulated secretion (6,7). Thus, the regulation of adiponectin secretion shows similarities with how hormone release is controlled in other endocrine cell types, although there are some fundamental differences (i.e. endocrine cell exocytosis is typically triggered by Ca^{2+} whereas cAMP has an amplifying effect on secretion (2)). Our results have clearly provided significant insight into the regulation of adiponectin exocytosis. However, the data contain information on mechanistic details that can only be fully retrieved using a mathematical modeling approach (8,9).

Several available mathematical models describe the regulation of Ca^{2+} -triggered exocytosis in traditional endocrine cell types, such as insulin-secreting beta cells (10-12), and catecholamine-releasing chromaffin cells

(13-15). Additional models have defined disease mechanisms related to white adipocytes insulin resistance (16-19). Clearly, a mathematical model specifically defining adiponectin exocytosis mechanisms is required to completely understand the mechanistic regulation of adiponectin release.

Here we use modeling as a tool to qualitatively and quantitatively evaluate and revise our current cell physiological understanding of how adiponectin exocytosis is regulated. Our prevailing concept of regulatory mechanisms (Fig. 1A, adapted from (6)) is updated in several steps resulting in a more detailed understanding of the adiponectin exocytosis process. Using the model to analyze data, we first show that the ATP-dependency of the functionally divided intracellular adiponectin vesicle pools needs to be formalized in a new way. We further show that endocytosis contributes to the measured capacitance signal and we are able to quantify the endocytosis contribution. By refinement of the model in several steps, we finally provide a revised and validated model of the molecular and cellular regulation of white adipocyte adiponectin release.

Results

Formal testing of hypotheses of adiponectin exocytosis regulatory mechanisms

To investigate the molecular and cellular mechanisms controlling adiponectin secretion, we have previously examined the role of the three intracellular mediators cAMP, Ca^{2+} , and ATP in 3T3-L1 adipocyte adiponectin exocytosis (6). Those mediators are known to have important roles in regulation of (neuro)endocrine cell secretion (2). In Komai et al 2014 (6), we performed whole-cell electrophysiological recordings of exocytosis by measuring the change in membrane capacitance, which corresponds to alterations of the cell surface area (increases with exocytosis and decreases with endocytosis).

Our key findings, confirmed in primary human subcutaneous adipocytes, were i) adiponectin exocytosis is triggered by cAMP and ii) a combination of Ca^{2+} and ATP potentially augments the cAMP-stimulated adiponectin vesicle release (Fig. 1A). To formally test our previous interpretations of experimental data, we have here directly translated this hypothesis (Fig. 1A) into a system of ordinary differential equations (ODEs). During the model development, all interactions were explicitly included, resulting in a model with three states corresponding to functionally diverse adiponectin vesicle pools (Fig. 1B): a reserve pool (Reserve), a releasable pool (Release), and a pool corresponding to vesicles undergoing exocytosis (Exocytosis). The original model contains 11 parameters that control the rate of the reactions between the states (Materials and Methods). These parameters are not possible to determine experimentally. We therefore used the time-series data in (6) with rates of exocytosis resulting from different inputs (i.e. perfusion of the interior of the patched cells with pipette solution containing or lacking cAMP, Ca^{2+} or ATP) to estimate parameter values. The pipette solutions contained 1) a combination of cAMP, Ca^{2+} and ATP; 2) cAMP together with Ca^{2+} ; 3) cAMP together with ATP and 4) cAMP alone (Fig. 2A-D). Despite extensive searches through the parameter space, we were unable to find agreement between the simulation of the original model (Fig. 2A-D, solid grey lines) and experimental data (Fig. 2A-D, black symbols \pm SEM) that passed a χ^2 -test. The model structure was therefore rejected (Exocytosis model – original, Table 1), and we concluded that the original model lacks important mechanisms and must be refined.

Refinement of the original hypothesis to include ATP-dependent replenishment of releasable vesicles

Analysis of the model simulations for the original hypothesis revealed that the dynamics of the cAMP, Ca^{2+} , and ATP input data, with a high peak and slow decrease in exocytotic rate ($\Delta C/\Delta t$; Fig. 2A, grey line), were not possible to fit concurrently with the lower peak in the cAMP and Ca^{2+} data set with ATP absent (Fig. 2B, grey line). This lack of agreement results from that the releasable vesicle pool in the original model is refilled by vesicles residing in the reserve pool as a function of Ca^{2+} alone (Fig. 1A and B). As a consequence, releasable vesicles would expectedly be depleted at a faster rate after the high exocytosis peak attained in the presence of ATP. Fig. 2E and F show model simulations of the remaining vesicles under the two conditions, as indicated. The observation that the releasable pool is rapidly depleted in the presence of ATP (Fig. 2E, grey lines) together with the lack of agreement in Fig. 2A and B indicate that ATP is involved in vesicle replenishment. The original hypothesis was therefore modified to contain an ATP-dependent term affecting the transition of vesicles from the reserve pool to the releasable pool (Fig. 2G, indicated in blue). This adjustment of the model is not in conflict with our original observations in (6), but merely represents another way to formalize the experimental findings. Inclusion of the ATP-dependency resulted in improved agreement between model simulations and experimental data (Fig. 2A-D, dashed blue lines). However, the model was still rejected by a χ^2 -test (Exocytosis model – ATP, Table 1).

To quantify the improvement resulting from the addition of the ATP-dependency, a likelihood ratio test was used to test the null-hypothesis that the models are equally good at describing the data. The extra parameter for the ATP-dependency decreased the χ^2 -error by 31 (from 62 to 31, Table 1). This should be compared to the threshold of 4 for 95% confidence and 1 degree of freedom (1 extra

parameter added to the model); i.e. the agreement with data improved more than the threshold value and the null-hypothesis was rejected. Thus, the added ATP-dependency step significantly improved the fit between the model and recorded data.

Inclusion of the contribution of endocytosis to the measured signal significantly improves the model

A remaining qualitative shortcoming is the inability of the model to capture the experimentally attained 25% lower peak of exocytotic rate in response to a combination of cAMP and Ca^{2+} (black symbols in Fig. 2B) compared to when exocytosis is triggered by cAMP alone (black symbols in Fig. 2D). This lower peak rate cannot be captured by a model structure including exclusively positive effects of Ca^{2+} on the measured signal. The membrane capacitance recordings denote the net result of cell exo- and endocytosis and Ca^{2+} has been shown to trigger both exo- and endocytosis in several peptide-secreting cell types (20-24). A very high intracellular free concentration of Ca^{2+} ($\geq 10 \mu\text{M}$) triggers endocytosis (i.e. affect capacitance measurements negatively) in a variety of (neuro)endocrine cell types (23,24).

In (6), we showed that a non-stimulatory (cAMP-lacking) pipette solution containing $1.5 \mu\text{M}$ free Ca^{2+} and ATP did not induce significant endocytosis even in experiments lasting as long as 20 minutes. With a few example traces, we further demonstrated that infusion of adipocytes with a pipette solution containing $\geq 10 \mu\text{M}$ free Ca^{2+} (20 mM CaCl_2 in combination with 10 mM of the Ca^{2+} chelator BAPTA) together with cAMP and ATP resulted in a lower exocytotic rate, interpreted as contribution of Ca^{2+} -dependent endocytosis (6). Those findings suggest that, in white adipocytes, cAMP stimulation of adiponectin exocytosis is required in order for Ca^{2+} -dependent endocytosis to occur.

Based on the above premises, we included a Ca^{2+} -dependent negative effect of Ca^{2+} on exocytosis in the form of endocytosis in the model (Fig. 3A). To experimentally quantify the effect of high Ca^{2+} on white adipocyte exo- and endocytosis, we infused 3T3-L1 adipocytes with the cAMP- and ATP-containing pipette solution supplemented with $\geq 10 \mu\text{M}$ free Ca^{2+} . Exocytosis was stimulated at a peak rate of $\Delta\text{C}/\Delta\text{t}=14\pm 1$ fF/s (measured at 2 min; Fig. 3B), thus at a significantly lower rate than triggered by the same solution containing $1.5 \mu\text{M}$ free Ca^{2+} ($\Delta\text{C}/\Delta\text{t}=21\pm 7$ fF/s; $p<0.01$; Fig. 2A). Our results indicate that an unphysiologically high intracellular Ca^{2+} concentration induces excessive endocytosis, manifested as a reduced measured exocytotic rate.

The positive effect of the increase from $1.5 \mu\text{M}$ to $\geq 10 \mu\text{M}$ Ca^{2+} does not display a linear relationship between Ca^{2+} concentration and exocytotic response (Fig. 3B) and thus needs to be saturated. Saturation was included in the model using a half-maximal saturation constant (Km):

$$v_{\text{Rel_Rel}} = \frac{\text{Ca}}{(\text{km} + \text{Ca})} * (\text{kCa2} + \text{kATP2} * \text{ATP}) * \text{Res}$$

$$v_{\text{Rel_Exo}} = \text{cAMP} * [\text{kbasal} + \text{kCaATP} * \frac{\text{Ca}}{(\text{km} + \text{Ca})} * \text{ATP}] * \text{Rel}$$

Note that saturation was not required for comparison of the original data sets (Fig. 2A-D) with a single free Ca^{2+} concentration.

Testing of the endocytosis-hypothesis confirmed agreement with data with high Ca^{2+} (Fig. 3B, black symbols \pm SEM) as well as data with $1.5 \mu\text{M}$ Ca^{2+} alone (Fig. 3C, black symbols \pm SEM). The developed model was also conformable with previous data sets (Fig. 2A-D) and we therefore gathered all

parameters that passed a χ^2 -test (Fig. 3B-G, orange areas).

Validation of the Exocytosis model – ATP/endocytosis model

To evaluate the model in Fig. 3A further, we used a new kind of experimental data consisting of accumulated adiponectin released into the media (measured by ELISA; 6). Intact 3T3-L1 adipocytes were incubated with a solution containing the cAMP-increasing agent forskolin in combination with the phosphodiesterase inhibitor IBMX (3-isobutyl-1-methylxanthine; FSK/IBMX) under different intracellular Ca^{2+} conditions (6). To ensure the agreement between the extracellular cAMP-elevating agents and infusion of cAMP via the patch pipette, we measured the effect of FSK/IBMX on membrane capacitance. FSK/IBMX potently stimulated exocytosis and the maximal $\Delta\text{c}/\Delta\text{t}$ averaged ~ 20 fF/s (Fig. 4). This rate is very similar to the exocytotic rate achieved upon infusion of cells with cAMP and $1.5 \mu\text{M}$ free Ca^{2+} (*cf.* Fig. 2A) thus justifying the usage of the secretion data for model validation.

The secretion data were attained using intact cells. Thus, cytoplasmic levels of intracellular mediators were, in contrast to the clamped conditions in the capacitance recordings, allowed to fluctuate. Consequently, the implementation of the secretion data in the adiponectin release model required an estimation of the intracellular levels of cAMP, ATP, and Ca^{2+} under the new experimental conditions.

By use of values in (6,7) we determined the basal intracellular Ca^{2+} concentrations ($[\text{Ca}^{2+}]_i$). Analysis gave a $[\text{Ca}^{2+}]_i$ interval of 35-230 nM (in agreement with reports from others (25)). In Komai et al 2014 (6), we found Ca^{2+} to increase 1.5-fold in the presence of FSK/IBMX. This combined information

allowed us to limit the range of Ca^{2+} concentrations in the model simulations.

The basal cAMP levels in adipocytes are low due to spontaneous release of adenosine (26). Absolute concentrations of adipocyte intracellular cAMP have never been described but Zu et al. reports basal cAMP in primary rat adipocytes to be ~ 6 pmol/mg protein (27). However, it is difficult to estimate how this value translates into actual cytoplasmic concentration, as that depends on the volume of the fat free mass and the protein content per cell. We therefore calculated the basal cAMP concentration in 3T3-L1 adipocytes from values reported in (6) and related those to the fat free mass (measured by coherent anti-Stokes Raman scattering and multi-photon excitation fluorescence; Table 2). The average basal cAMP concentration was calculated to be $55 \mu\text{M}$. The lowest measured value was $2 \mu\text{M}$ (Table 2), in the same range as concentrations reported in cardiomyocytes ($1.2\text{-}1.3 \mu\text{M}$; 28,29). Our capacitance measurements show that $100 \mu\text{M}$ cAMP stimulates adiponectin exocytosis (6). Thus, the basal intracellular cAMP concentration was allowed to range between 2 and $100 \mu\text{M}$ when predicting the secretion experiments.

We have previously shown that FSK/IBMX increases 3T3-L1 adipocyte intracellular cAMP levels ~ 6.5 -fold (unaffected by BAPTA treatment; 6); we implemented this constraint in the model.

The intracellular ATP levels in fully differentiated 3T3-L1 adipocytes exposed to a physiological glucose concentration are unknown. Hresko et al. (30) have reported an ATP concentration of ~ 5 mM in 3T3-L1 adipocytes. However, this value was measured in cells exposed to high glucose (25 mM, likely resulting in enhanced ATP production) and is therefore difficult to compare to our experiments carried out at a basal (5 mM)

glucose concentration. Due to lack of experimental constraints, and to avoid underestimation of the uncertainty of the prediction, we allowed for a wide variety of ATP levels in the model simulations ($1 \mu\text{M} - 1 \text{mM}$) regardless of treatment conditions. The basal cytosolic ATP concentration has been reported to be 1 mM in clonal beta-cells (31), thus in agreement with our range of cytosolic ATP.

We used the determined intervals of intracellular Ca^{2+} , cAMP, and ATP and an approximation of all found acceptable parameters to simulate the adiponectin accumulation after stimulation with FSK/IBMX alone, FSK/IBMX after pre-treatment with the Ca^{2+} chelator BAPTA and FSK/IBMX together with the Ca^{2+} ionophore ionomycin (Fig. 5A, filled area). We compared the simulated 30 min time point (Fig. 5A, black boxes, summarized in 5B) with real adiponectin secretion (Fig. 5C), measured as accumulated adiponectin in the media under the same experimental conditions (6). The simulations were found to closely resemble the data (*cf.* Fig. 5B and 5C). To simulate the effect of ionomycin we allowed the Ca^{2+} concentration to increase at least 1.5 times with ionomycin, and maximally 10 times above basal levels with FSK/IBMX in combination with ionomycin.

To further validate the model, in a dynamic setting, we studied the time-resolved prediction of FSK/IBMX-stimulated adiponectin secretion at 15, 30, 45, and 60 minutes. The predictions with corresponding uncertainties show a clear nonlinear behaviour with saturation (Fig. 5D). We performed the corresponding experiments of FSK/IBMX-stimulated adiponectin secretion, measured at the simulated time-points. As shown in Fig. 5E, there was a distinct resemblance between simulated and real data. It is noteworthy that although the model was

developed using capacitance recordings restricted to a time-period of 12 min, it is capable of simulating the dynamic adiponectin secretion at several-fold longer time points.

Quantification of the contribution of Ca^{2+} - dependent endocytosis to the exocytosis measurements

Using the validated model, we predicted the contribution of endocytosis to the measured signal under different experimental conditions (Fig. 6A). To determine the interval of possible contribution using the uncertainty of data, we used two global optimization algorithms (Materials and Methods) to collect different parameter sets (all yielding simulations in agreement with data within a 95% confidence interval) (8). The contribution of endocytosis to the measured signal was found to be i) 21 ± 12 % with cAMP, $1.5 \mu\text{M}$ Ca^{2+} , and ATP, ii) 29 ± 13 % with cAMP and $1.5 \mu\text{M}$ Ca^{2+} (ATP excluded), and iii) 42 ± 5 % in experiments with $\geq 10 \mu\text{M}$ Ca^{2+} added together with cAMP and ATP (Fig. 6). As expected, the contribution of endocytosis to the capacitance measurements is most pronounced at exceedingly elevated Ca^{2+} concentrations.

Discussion

Here we use a combined experimental and mathematical modeling approach to investigate the mechanisms regulating white adipocyte adiponectin secretion. We present the first mathematical model of adiponectin exocytosis. By taking advantage of both previously published and newly generated data, we draw quantitative conclusions that would have been impossible to assess without modeling.

Ca^{2+} -dependent endocytosis ensues simultaneously with exocytosis

The final model equations can be translated back to a biological interaction graph that summarizes our findings (Fig. 7). We conclude that, i) the redistribution of vesicles from the Reserve pool to the Releasable pool includes an ATP-dependent component, ii) a negative effect of Ca^{2+} , in the form of endocytosis, is needed to explain the capacitance measurements. The ability to quantify the contribution of endocytosis to recorded capacitance increases is essential for the interpretation of our adiponectin exocytosis studies. Importantly, the model presented here show that we may underestimate the magnitude of adiponectin exocytosis in the presence of a physiologically relevant intracellular Ca^{2+} concentration and that the potentiating effect of Ca^{2+} on cAMP-stimulated adiponectin secretion is larger than displayed in our electrophysiological recordings (6). The finding that Ca^{2+} -dependent endocytosis depends on the simultaneous presence of cAMP does not signify that endocytosis as such requires the presence of the cyclic nucleotide per se, but rather designates that endocytosis (plasma membrane retrieval) needs to be preceded by exocytosis (plasma membrane enlargement). The observation that the contribution of endocytosis is pronounced in the presence of $\geq 10 \mu\text{M}$ free Ca^{2+} (Fig. 6A) emphasises the importance of performing the capacitance measurements under physiologically relevant conditions (thus in the intracellular presence of appropriate levels of mediators known to affect exocytosis). We found that the membrane retrieval was unaffected by intracellular ATP. This is in agreement with results in other peptide secreting cell types such as rat corticotrophs (32) and mouse β -cells (33) where endocytosis has likewise been shown to proceed uniformly in the absence or presence of the nucleotide. Moreover, the lack of ATP-dependency suggests that the endocytosis following cAMP-stimulated adiponectin secretion does not depend on

protein phosphorylation. The magnitude of Ca^{2+} -dependent endocytosis may appear rather large also under physiologically relevant conditions ($\geq 20\%$ Fig. 6B). However, the percentage of the measured signal corresponding to endocytosis predicted using our model is low compared to calculated ratio of endocytosis/exocytosis after stimulated exocytosis in rat corticotrophs (32).

The developed model can predict adiponectin secretion/exocytosis

In the validation of the final model structure, we used all acceptable parameters that were justified for the new experimental conditions (see Results) to include the uncertainty of the data in model predictions. This approach is important, since the optimal parameters and other acceptable parameters might give different, but still plausible predictions for new data. We find that the developed model is able to predict adiponectin secretion under several different stimulatory conditions and at protracted time-points in dynamic experiments (Fig. 5D and E) This suggests that the model can in the future be used to predict whole-cell membrane capacitance responses at late time-points that are methodologically challenging to measure experimentally, even though such analyses require further validation. Moreover, the finding that simulations of adiponectin secretion so accurately predicts experimental results strengthens our proposal that adipocyte membrane capacitance increases in response to cAMP, with or without Ca^{2+} , signify adiponectin vesicle fusion with the plasma membrane (6,7).

We want to emphasise that although the model is in agreement with both estimations and validation data, there could be other models able to explain the data equally well. The developed model is, however, useful since it is i) a minimal model based on current biological knowledge, ii) reached after several rejections of simpler models, and iii) currently the only existing model of adiponectin secretion. We

encourage that our model is further advanced, by us or by others, when more data become available.

Using models to understand the pathophysiology of adiponectin exocytosis in metabolic disease

Recent work from our group has enhanced our understanding of adiponectin exocytosis in health and in metabolic disease. Using subcutaneous white adipocytes isolated from lean or obese/diabetic mice, we have shown that adiponectin exocytosis is stimulated by catecholamines (elevates cytoplasmic cAMP) and that the stimulation mainly involves activation of β_3 adrenergic receptors. Moreover, adipocytes isolated from obese/diabetic mice display blunted catecholamine-stimulated adiponectin secretion in a state we define as *catecholamine resistance*. The blunted release is due to a secretory defect and does not result from reduced intracellular adiponectin content (34). To improve our understanding of the mechanistic details involved in adrenergically stimulated adiponectin exocytosis under pathophysiological conditions, it is necessary to further analyze the experimental data by use of a modeling approach.

The adiponectin secretion model presented in Fig. 7 can in the future be combined with models describing other cellular processes and functions in white adipocytes, e.g. the detailed insulin signalling and glucose uptake model in (17). Moreover, our adiponectin secretion model can be extended and included in a state-of-the-art multi-level model where interactions are studied on cellular, organ, and systemic levels. Such a convoluted model, where metabolic signalling pathways are continuously added, has already been developed for the glucose and insulin system (16,35). Complex models of the regulation of whole body physiology, with ensuing additions of more regulators and sub-systems,

are essential to enhance our understanding of pathophysiological metabolic conditions.

Experimental procedures

Mathematical modeling

All mathematical analyzes, *i.e.* simulations and optimizations, were carried out in MATLAB R2016a using IQM tools (a continuation of the SBtoolbox2 package (36,37) and the MATLAB Global Optimization toolbox. A combination of the Global Optimization toolbox algorithms; particleswarm, fmincon and simulannealbnd; were used to estimate the parameters. Models were based on ordinary differential equations (ODE) and reactions were assumed to mainly follow mass action kinetics (see exceptions below). Rate constants are referred to as parameters, *i.e.* values that change the model output. Evaluation of parameters was done by simulating the model using IQM tools and then calculating the χ^2 -error accordingly:

$$Cost(p) = \sum_{i=1}^m \frac{(y_i(t) - \hat{y}_i(t,p))^2}{SEM_i(t)^2}$$

Here, y denotes the measured data, \hat{y} denotes the model simulation to compare with data, SEM denotes the standard error of the mean, t denotes the measured time points and p denotes the model parameters. The sum is over all measured time points for all datasets. The calculated sum follows a χ^2 distribution. Therefore, χ^2 tests were used to determine model rejections (38). We used a significance level of 0.05, and the number of degrees of freedom equals the number of data points minus one parameter for normalization and minus the number of parameters in the model. For the time-series data (Fig. 2A-D) with $n = 7 \cdot 4 = 28$ data points, the border of rejections for the original model with 11

parameters is given by the inverse cumulative χ^2 (28-1-11, 0.05) = 26.

All model files and code to simulate the models are available at github.com/elinnyman/adiponectin-secretion.

Detailed description of the developed model

We aimed to develop a mathematical model that describes all our data for adiponectin secretion in adipocytes in an acceptable manner. We limited the scope and the size of the model to the available data to keep the estimation of parameters as simple as possible. The developed ODE model consists of two parts: the input equations and the actual adiponectin secretion model. The input equations describe the intracellular dynamics of Ca^{2+} , ATP, and cAMP after infusion via the pipette solution. These equations all have the same format:

$$d/dt(\mathbf{Ca}) = kCa * (-Ca + basalCa + (targetCa - basalCa) * kattach)$$

$$d/dt(\mathbf{ATP}) = kATP * (-ATP + basalATP + (targetATP - basalATP) * kattach)$$

$$d/dt(\mathbf{cAMP}) = kcAMP * (-cAMP + basalcAMP + (targetcAMP - basalcAMP) * kattach)$$

$$\mathbf{Ca}(0) = basalCa$$

$$\mathbf{ATP}(0) = basalATP$$

$$\mathbf{cAMP}(0) = basalcAMP$$

The states of the model are marked in bold. All input equations have the same format. As an example, the details of the Ca equation are as follows. In the steady-state simulation, kattach is set to 0, and when the pipette is attached to the cell, kattach changes from 0 to 1. The state Ca corresponds to the intracellular concentration of Ca. basalCa is the desired concentration of Ca in steady-state (before attachment of the pipette) and targetCa is the

desired final concentration after attachment of the pipette.

The parameters for these equations were allowed to vary within certain limits during the parameter estimation, to give some flexibility in the input dynamics. kCa was limited to 0.0035 - 0.7, to give a half-maximal response time roughly between 1 - 200 seconds. $kATP$ and $kCaMP$ were allowed to vary 10% from kCa . $basalCa$ where allowed to vary between 35-230 nM, $basalATP$ between 1 μ M – 1 M, and $basalCaMP$ between 1 nM – 0.1 M. The target values ($targetCa$, $targetATP$ and $targetCaMP$) where changed to match the experimental protocol.

The adiponectin secretion model consists of three states:

$$\begin{aligned} \frac{d}{dt}(\mathbf{Res}) &= 0 \\ \frac{d}{dt}(\mathbf{Rel}) &= v_{Res_Rel} - v_{Rel_Exo} + v_{Exo_Rel} \\ \frac{d}{dt}(\mathbf{Exo}) &= v_{Rel_Exo} - v_{Exo_Rel} - v_{Exo} \\ \mathbf{Res}(0) &= Res0 \\ \mathbf{Rel}(0) &= Rel0 \\ \mathbf{Exo}(0) &= Exo0 \end{aligned}$$

where Res is the Reserve Pool of vesicles, assumed to be in high abundance compared to the other pools of vesicles and thus assumed not to change over time. Rel is the Releasable Pool of vesicles, and Exo the state of vesicles undergoing exocytosis. $Res0$ was chosen to be an arbitrary number and the equations for $Rel0$ and $Exo0$ were derived by setting the ODEs to zero (i.e. force steady state) and then solving the system of equations. This gives the following equations:

$$\begin{aligned} Res0 &= 97 \\ Rel0 &= basalCa / (km + basalCa) * (kCa2 + kATP2 * basalATP) * Res0 * (1 + \end{aligned}$$

$$\begin{aligned} &krel / kexo) / [basalCaMP * (kbasal + basalCa / (km + basalCa) * basalATP * kCaATP)] \\ Exo0 &= basalCa / (km + basalCa) * (kCa2 + kATP2 * basalATP) * Res0 / kexo \\ Endo0 &= kCacAMP * (basalCaMP * basalCa) / kEndo \end{aligned}$$

The reaction rates for the original model are:

$$\begin{aligned} v_{Res_Rel} &= kCa2 * Ca * Res \\ v_{Rel_Exo} &= CaMP * (kbasal + kCaATP * Ca * ATP) * Rel \\ v_{Exo_Rel} &= krel * Exo \\ v_{Exo} &= kexo * Exo \end{aligned}$$

The reaction rate from the state Exo (v_{Exo}) corresponds to the measured rate of change to compare with the capacitance measurements. A scaling parameter was used for transition to the unit less model to the unit in the measurements (fF/s):

$$u = kscale * v_{Exo}$$

In the Exocytosis model – ATP, we modified the original model to include an extra ATP-dependency with an ATP-dependency of the reaction from Reserve pool to Releasable pool:

$$v_{Res_Rel} = Ca * (kCa2 + kATP2 * ATP) * Res$$

In the Exocytosis model – ATP/endocytosis model, the dynamics of the endocytotic vesicles are described by:

$$\begin{aligned} \frac{d}{dt}(\mathbf{Endo}) &= v_{Ca_Endo_} - v_{Endo} \\ \mathbf{Endo}(0) &= Endo0 = kCacAMP * (basalCaMP * basalCa) / kEndo \end{aligned}$$

The corresponding reaction rates are:

$$vCa_Endo = kCacAMP * Ca * cAMP$$

$$vEndo = kendo * Endo$$

The difference between the reaction rates ($v_{Exo} - v_{Endo}$) was used to compare as the measured rate of change in the capacitance measurements in the endocytosis model. With a scaling parameter, the model output thus converts to:

$$u = kscale * (v_{Exo} - v_{Endo})$$

To be able to fit the data with high concentration of Ca^{2+} , a saturation effect was added to the positive Ca^{2+} effects:

$$vRes_Rel = \frac{Ca}{(km + Ca)} * (kCa2 + kATP2 * ATP) * Res$$

$$vRel_Exo = \frac{cAMP * [kbasal2 + kCaATP * Ca]}{(km + Ca) * ATP} * Rel$$

Model validation

In the model validation, we used the model to predict experimental data not used in the parameter estimation (measurements of accumulated released adiponectin). The model output that we compare to data is:

$$u = Exo(input) / Exo(control)$$

We simulated the final model using all acceptable parameters, i.e. all found parameters that gave model simulations that passed a χ^2 test. Instead of the previously used input equations for Ca^{2+} , ATP, and cAMP, we used a wide range of values to simulate the predictions (see the Results section for motivation of the intervals). We also added 25 % uncertainty to the intervals.

Basal intervals:

$$Ca^{2+}: 0.035 - 0.23 \mu M$$

$$ATP: 0.001 - 1 mM$$

$$cAMP: 10^{-6} - 0.1 mM$$

FSK/IBMX simulation:

$$Ca^{2+} = basal * (1.5 \pm 0.25)$$

$$cAMP = basal * (6.5 \pm 0.25)$$

$$ATP = basal$$

FSK/IBMX + BAPTA simulation:

$$Ca^{2+} = 0$$

$$cAMP = basal * (6.5 \pm 0.25)$$

$$ATP = basal$$

FSK/IBMX + Ionomycin simulation:

$$Ca^{2+} = basal * (3 \pm 0.25) - basal * 10$$

$$cAMP = basal * (6.5 \pm 0.25)$$

$$ATP = basal$$

To simulate the model predictions, we sampled from all acceptable parameters and used the max and the min values of the above intervals in all possible combinations to explore the entire interval of predictions.

Prediction of endocytosis contribution

In the evaluation of the contribution of endocytosis to the measured signal, the calculated ratio between the rate of endocytosis and the sum of endocytosis and exocytosis was multiplied times 100 to get the contribution in %:

$$Endo_ratio = \frac{v_{Endo}}{(v_{Exo} + v_{Endo})} * 100$$

To calculate the intervals of the contribution (Fig. 6A-B), we performed parameter searches in the direction of this specific prediction (7).

χ -error for each value of the prediction is shown in the figures (Fig. 6B).

Experimental methods

All experimental data, with the exception of that presented in (Fig. 3A-B and 5E) and Table 2 are adapted from (6). The data in (6) consist of whole-cell patch-clamp recordings and ELISA measurements of secreted adiponectin. 3T3-L1 adipocytes were differentiated as previously described (6,7).

Electrophysiology

3T3-L1 adipocytes, grown in plastic (Nunc, Denmark) Petri culture dishes, were continuously superfused during the recordings with an extracellular solution (EC) containing (in mM): 140 NaCl, 3.6 KCl, 2 NaHCO₃, 0.5 NaH₂PO₄, 0.5 MgSO₄, 5 Hepes (pH 7.4 with NaOH), 2.6 CaCl₂ supplemented with 5 mM glucose. 3T3-L1 adipocyte exocytosis was measured as increase in membrane capacitance using an EPC-9 patch-clamp amplifier (HEKA Electronics, Lambrecht/Pfalz, Germany) and PatchMaster software. A fire-polished borosilicate glass pipette was attached to cells by gentle suction and electrical access attained by rupture of the plasma membrane within the patch. Consequently, the pipette filling solution (containing indicated concentrations of cAMP, ATP and/or Ca²⁺) equilibrates with the cytosol. Cells were voltage-clamped at -70 mV. The pipette-filling solutions contained (in mM): 125 potassium glutamate, 10 KCl, 10 NaCl, 1 MgCl₂, 5 Hepes (pH 7.15 with KOH) and were supplemented with cAMP, ATP and Ca²⁺ as indicated. Exocytotic rates ($\Delta C/\Delta t$) were measured by applying a linear fit to the capacitance trace at different time points and calculate the slope of the fitted line. For more details, see (6).

Measurements of released adiponectin

Secreted total adiponectin was measured using 3T3-L1 adipocytes grown on 12-well plates (Sarstedt) stimulated with EC containing

indicated secretagogues during 15-60 minute incubations at 32°C, as previously described (Komai 2016). EC aliquots and cell homogenates were stored at -80°C. Secreted adiponectin (measured with mouse ELISA DuoSets; R&D Systems) was analyzed in relation to total protein content (Bradford protein assay).

CARS & MPEF microscopy.

Live differentiated cells were stained with 2 μ M CellTracker™ Red CMTPX Dye (MolecularProbes™, Thermo Fischer Scientific) in serum-free medium for 30 minutes at 37°C. The lipid content of the living cells was determined (Fig. 8) with combined coherent anti-Stokes Raman scattering (CARS) and multi-photon excitation fluorescence (MPEF) microscopy on a custom-build setup (39). The 2845 cm⁻¹ C-H stretching vibrations of triglycerides were driven with a spatially and temporal overlap of two picosecond-pulsed laser beams (816.9 nm and 1064 nm, 7ps, 76 MHz, Nd:Vanadate, HighQ, pumped Levante Emerald OPO, APE Berlin) in the focal plane of an inverted microscope (Eclipse TE2000-E with a C2 Confocal Microscope scanning head, Nikon) using an oil immersion objective (Nikon Plan Fluor, 40 \times NA 1.30). The cytosolic fluorescence probe was simultaneously excited with the 816.9nm beam. Single photon counting detectors (Becker&Hickl GmbH) coupled with dichroic mirrors and bandpass filters (Semrock) were used to detect CARS signals in forward direction (BP 661/20nm) and MPEF signals in epi direction (609/57nm). Five images with 5.04 μ s pixel dwell time were summed for each acquisition. Individual cells were identified from the combined MPEF and CARS images and their size measured. The lipid signal per cell was separated, thresholded (RenyEntropy algorithm) using ImageJ (the National Institutes of Health, USA), and also measured in size. Assuming a

spherical shape, the cell and lipid volume can be estimated from the area (20 cells x 3 technical repeats; Fig. 8).

Confocal microscopy

Fully differentiated 3T3-L1 cells were fixed in 4% paraformaldehyde, stained with Hoechst (34580, Molecular Probes) and imaged using a Nikon Ti-E microscope. The images were analyzed (nuclear count) using Fiji/Image J.

Acknowledgements

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Competing Interests

AstraZeneca provided support in the form of salary for author EN.

Author Contributions

CB planned the study, performed experiments, analyzed models and data, and wrote the paper. WL performed modeling and contributed to the writing of the manuscript. AP performed experiments, analyzed data and contributed to the writing of the manuscript. AK performed experiments and analyzed data. TA performed modeling and contributed to the writing of the manuscript. MF. EH performed experiments and analyzed data. EN planned the study, performed modeling, analyzed models and wrote the manuscript. CO planned experiments, analyzed data, and wrote the manuscript and contributed reagents and material. All authors have read, edited and approved of the final version of the manuscript.

References

1. Li, S., Shin, H. J., Ding, E. L., and van Dam, R. M. (2009) Adiponectin levels and risk of type 2 diabetes: a systematic review and meta-analysis. *Jama* **302**, 179-188
2. Burgoyne, R. D., and Morgan, A. (2003) Secretory granule exocytosis. *Physiol Rev* **83**, 581-632
3. Bogan, J. S., and Lodish, H. F. (1999) Two Compartments for Insulin-Stimulated Exocytosis in 3t3-L1 Adipocytes Defined by Endogenous Acrp30 and Glut4. *J Cell Biol.* **146**, 609-620
4. Xie, L., O'Reilly, C. P., Chapes, S. K., and Mora, S. (2008) Adiponectin and leptin are secreted through distinct trafficking pathways in adipocytes. *Biochim Biophys Acta* **1782**, 99-108
5. Bose, A., Guilherme, A., Huang, S., Hubbard, A. C., Lane, C. R., Soriano, N. A., and Czech, M. P. (2005) The v-SNARE Vti1a regulates insulin-stimulated glucose transport and Acrp30 secretion in 3T3-L1 adipocytes. *J. Biol. Chem.* **280**, 36946-36951

6. Komai, A. M., Brannmark, C., Musovic, S., and Olofsson, C. S. (2014) PKA-independent cAMP stimulation of white adipocyte exocytosis and adipokine secretion: modulations by Ca²⁺ and ATP. *J Physiol.* **592**, 5169-5186
7. El Hachmane, M. F., Komai, A. M., and Olofsson, C. S. (2015) Cooling reduces cAMP-stimulated exocytosis and adiponectin secretion at a Ca²⁺-dependent step in 3T3-L1 adipocytes. *PLoS One* **10**, e0119530
8. Cedersund, G. (2012) Conclusions via unique predictions obtained despite unidentifiability--new definitions and a general method. *FEBS J* **279**, 3513-3527
9. Nyman, E., Lindgren, I., Lovfors, W., Lundengard, K., Cervin, I., Sjostrom, T. A., Altimiras, J., and Cedersund, G. (2015) Mathematical modeling improves EC50 estimations from classical dose-response curves. *FEBS J* **282**, 951-962
10. Galvanovskis, J., Braun, M., and Rorsman, P. (2011) Exocytosis from pancreatic β -cells: mathematical modelling of the exit of low-molecular-weight granule content. *Interface Focus* **1**, 143-152
11. Goforth, P. B., Bertram, R., Khan, F. A., Zhang, M., Sherman, A., and Satin, L. S. (2002) Calcium-activated K⁺ Channels of Mouse β -cells are Controlled by Both Store and Cytoplasmic Ca²⁺: Experimental and Theoretical Studies. *J Gen Physiol* **120**, 307-322
12. Keizer, J., and Magnus, G. (1989) ATP-sensitive potassium channel and bursting in the pancreatic beta cell. A theoretical study. *Biophys J* **56**, 229-242
13. Amatore, C., Bouret, Y., Travis, E. R., and Wightman, R. M. (2000) Interplay between membrane dynamics, diffusion and swelling pressure governs individual vesicular exocytotic events during release of adrenaline by chromaffin cells. *Biochimie* **82**, 481-496
14. Jarukanont, D., Bonifas Arredondo, I., Femat, R., and Garcia, M. E. (2015) Vesicle Motion during Sustained Exocytosis in Chromaffin Cells: Numerical Model Based on Amperometric Measurements. *PLoS One* **10**, e0144045
15. Sun, L., Xiong, Y., Zeng, X., Wu, Y., Pan, N., Lingle, C. J., Qu, A., and Ding, J. (2009) Differential regulation of action potentials by inactivating and noninactivating BK channels in rat adrenal chromaffin cells. *Biophys J* **97**, 1832-1842
16. Brannmark, C., Nyman, E., Fagerholm, S., Bergenholm, L., Ekstrand, E. M., Cedersund, G., and Stralfors, P. (2013) Insulin signaling in type 2 diabetes: experimental and modeling analyses reveal mechanisms of insulin resistance in human adipocytes. *J. Biol. Chem.* **288**, 9867-9880
17. Nyman, E., Rajan, M. R., Fagerholm, S., Brannmark, C., Cedersund, G., and Stralfors, P. (2014) A Single Mechanism Can Explain Network-wide Insulin Resistance in Adipocytes from Obese Patients with Type 2 Diabetes. *J. Biol. Chem.* **289**, 33215-33230
18. Sips, F. L., Nyman, E., Adiels, M., Hilbers, P. A., Stralfors, P., van Riel, N. A., and Cedersund, G. (2015) Model-Based Quantification of the Systemic Interplay between Glucose and Fatty Acids in the Postprandial State. *PLoS One* **10**, e0135665
19. Rajan, M. R., Nyman, E., Kjolhede, P., Cedersund, G., and Stralfors, P. (2016) Systems-wide Experimental and Modeling Analysis of Insulin Signaling through Forkhead Box Protein O1 (FOXO1) in Human Adipocytes, Normally and in Type 2 Diabetes. *J. Biol. Chem.* **291**, 15806-15819
20. Artalejo, C. R., Henley, J. R., McNiven, M. A., and Palfrey, H. C. (1995) Rapid endocytosis coupled to exocytosis in adrenal chromaffin cells involves Ca²⁺, GTP, and dynamin but not clathrin. *Proc Natl Acad Sci U S A* **92**, 8328-8332
21. Engisch, K. L., and Nowycky, M. C. (1998) Compensatory and excess retrieval: two types of endocytosis following single step depolarizations in bovine adrenal chromaffin cells. *J Physiol.* **506**, 591-608
22. Hosoi, N., Holt, M., and Sakaba, T. (2009) Calcium Dependence of Exo- and Endocytotic Coupling at a Glutamatergic Synapse. *Neuron* **63**, 216-229
23. Sun, T., Wu, X. S., Xu, J., McNeil, B. D., Pang, Z. P., Yang, W., Bai, L., Qadri, S., Molkentin, J. D., Yue, D. T., and Wu, L. G. (2010) The role of calcium/calmodulin-activated calcineurin in rapid and slow endocytosis at central synapses. *J Neurosci* **30**, 11838-11847

24. He, Z., Fan, J., Kang, L., Lu, J., Xue, Y., Xu, P., Xu, T., and Chen, L. (2008) Ca²⁺ Triggers a Novel Clathrin-Independent but Actin-Dependent Fast Endocytosis in Pancreatic Beta Cells. *Traffic* **9**, 910-923
25. Klip, A., and Ramlal, T. (1987) Cytoplasmic Ca²⁺ during differentiation of 3T3-L1 adipocytes. Effect of insulin and relation to glucose transport. *J. Biol. Chem.* **262**, 9141-9146
26. Schwabe, U., Ebert, R., and Erbler, H. C. (1973) Adenosine release from isolated fat cells and its significance for the effects of hormones on cyclic 3',5'-AMP levels and lipolysis. *Naunyn Schmiedebergs Arch Pharmacol.* **276**, 133-148
27. Zu, L., Jiang, H., He, J., Xu, C., Pu, S., Liu, M., and Xu, G. (2008) Salicylate Blocks Lipolytic Actions of Tumor Necrosis Factor- α in Primary Rat Adipocytes. *Mol Pharmacol.* **73**, 215-223
28. Borner, S., Schwede, F., Schlipp, A., Berisha, F., Calebiro, D., Lohse, M. J., and Nikolaev, V. O. (2011) FRET measurements of intracellular cAMP concentrations and cAMP analog permeability in intact cells. *Nat. Protocols* **6**, 427-438
29. Iancu, R. V., Ramamurthy, G., Warriar, S., Nikolaev, V. O., Lohse, M. J., Jones, S. W., and Harvey, R. D. (2008) Cytoplasmic cAMP concentrations in intact cardiac myocytes. *Am J Physiol Cell Physiol.* **295**, C414-C422
30. Hresko, R. C., Heimberg, H., Chi, M. M., and Mueckler, M. (1998) Glucosamine-induced insulin resistance in 3T3-L1 adipocytes is caused by depletion of intracellular ATP. *The J. Biol. Chem.* **273**, 20658-20668
31. Kennedy, H. J., Pouli, A. E., Ainscow, E. K., Jouaville, L. S., Rizzuto, R., and Rutter, G. A. (1999) Glucose generates sub-plasma membrane ATP microdomains in single islet beta-cells. Potential role for strategically located mitochondria. *J. Biol. Chem.* **274**, 13281-13291
32. Lee, A. K., and Tse, A. (2001) Endocytosis in identified rat corticotrophs. *J Physiol.* **533**, 389-405
33. Eliasson, L., Proks, P., Ammala, C., Ashcroft, F. M., Bokvist, K., Renstrom, E., Rorsman, P., and Smith, P. A. (1996) Endocytosis of secretory granules in mouse pancreatic beta-cells evoked by transient elevation of cytosolic calcium. *J Physiol.* **493 (Pt 3)**, 755-767
34. Komai, A. M., Musovic, S., Peris, E., Alrifaiy, A., El Hachmane, M. F., Johansson, M., Asterholm, I. W., and Olofsson, C. S. (2016) White Adipocyte Adiponectin Exocytosis is Stimulated Via beta3 Adrenergic Signaling and Activation of Epac1: Catecholamine Resistance in Obesity and Type 2 Diabetes. *Diabetes*
35. Nyman, E., Brännmark, C., Palmér, R., Brugård, J., Nyström, F. H., Strålfors, P., and Cedersund, G. (2011) A hierarchical whole-body modeling approach elucidates the link between in Vitro insulin signaling and in Vivo glucose homeostasis. *J. Biol. Chem.* **286**, 26028-26041
36. Schmidt, H., and Jirstrand, M. (2006) Systems Biology Toolbox for MATLAB: a computational platform for research in systems biology. *Bioinformatics* **22**, 514-515
37. Schmidt, H. (2007) SBaddon: high performance simulation for the Systems Biology Toolbox for MATLAB. *Bioinformatics* **23**, 646-647
38. Cedersund, G., Roll, J., Ulfhielm, E., Danielsson, A., Tidefelt, H., and Strålfors, P. (2008) Model-Based Hypothesis Testing of Key Mechanisms in Initial Phase of Insulin Signaling. *PLoS Comput Biol* **4**, e1000096
39. Brackmann, C., Gabrielsson, B., Svedberg, F., Holmaang, A., Sandberg, A. S., and Enejder, A. (2010) Nonlinear microscopy of lipid storage and fibrosis in muscle and liver tissues of mice fed high-fat diets. *J Biomed Opt* **15**, 066008

Table 1: Summary of all model evaluations The threshold for the χ^2 -error for 95 % significance is calculated using the number of data points (28 in the original data and 39 in the extended data) minus 1 normalization parameter minus the number of parameters in the model.

	Agreement with original data (χ^2 -error; threshold)	Conclusion from original data agreement	Agreement with extended data (original data + >10 μM free Ca^{2+} + 0 cAMP) (χ^2 -error; threshold)	Final conclusion
Exocytosis model – original (11 parameters)	62 (>26)	Rejected	-	Rejected
Exocytosis model – ATP (12 parameters)	31 (>25)	Rejected	-	Rejected
Exocytosis model – ATP/endocytosis (15 parameters)	11 (<21)	Not rejected	20 (<35)	Agreement with all data

Table 2: Calculation of 3T3-L1 adipocyte intracellular cAMP concentration Values of cAMP were taken from (6). 3T3-L1 cells were seeded and differentiated as described in the materials and methods section. Number of cells, cell volume and lipid volume was calculated using a nuclear stain (DAPI), MPEF and CARS.

cAMP / well (ng)	Cell number / well	Cell volume / cell (pL)	Lipid volume / cell (pL)	Lipid free volume / cell (pL)	Resulting cAMP
47.3 \pm 6.4	72263.7 \pm 2233.7	49.0 \pm 4.4	9.0 \pm 0.77	40.0 \pm 3.9	55 μM (range 1.98-175 μM)
Mean of 44 wells	Mean of 12 wells	Mean of 60 cells	Mean of 60 cells	Mean of 60 cells	

Figure legends

Figure 1: Biological insights formally tested using mathematical modeling

A) Biological insights adapted from (6). In brief, adiponectin vesicle exocytosis is triggered by cAMP alone but is augmented by the combined presence of ATP and Ca^{2+} . Moreover, Ca^{2+} -dependent mechanisms recruit vesicles to a functional pool from where they can be released (vesicles become release competent). B) The developed original mathematical model with 11 free parameters. Large arrows represent transitions between the different vesicle states and smaller arrows indicate model inputs. The rate of exocytosis in the model is compared to the experimentally measured rate of capacitance change.

Figure 2: Vesicle recruitment to the releasable pool must be ATP-dependent

Exocytotic rates ($\Delta C/\Delta t$) measured at indicated time points, as described in (6). Simulations of the original model are shown as grey lines and the refined model with ATP-dependency is indicated by dashed blue lines. A-D) Model simulations and capacitance recordings from (6; black circles \pm SEM) in fully differentiated 3T3-L1 adipocytes infused with pipette solutions containing or lacking 0.1 mM cAMP, 3 mM ATP or 1.5 μM Ca^{2+} , as indicated. In C and D, absolute intracellular Ca^{2+} free conditions were ascertained by inclusion of 10 mM of the Ca^{2+} chelator BAPTA in the pipette solution. E-F) Model simulations of the remaining vesicles in the releasable pool after addition of cAMP, Ca^{2+} and ATP (E) or cAMP and Ca^{2+} without ATP (F). G) The structure of the refined model with ATP-dependency (dashed blue arrow) including 12 free parameters.

Figure 3: The contribution of Ca^{2+} -dependent endocytosis to the capacitance measurements improves the model

A) The structure of the endocytosis model with 15 free parameters. The difference between the rate of exocytosis and endocytosis in the model is compared to the experimentally measured rate of capacitance change. B) $\Delta C/\Delta t$ in cells infused with a solution containing $\geq 10 \mu\text{M}$ free Ca^{2+} together with 3 mM ATP and 0.1 mM cAMP. The average exocytotic rate ($\Delta C/\Delta t$) was quantified at indicated time points. Results are an average from 11 recordings. C) Data from (6) with a pipette solution lacking cAMP (1.5 μM Ca^{2+} and 3 mM ATP included). The average $\Delta C/\Delta t$ was quantified at the designated time points. D-G) Data from (6); see Fig. 2 A-D for details.

Figure 4: Exocytosis induced by extracellular forskolin together with IBMX resembles that stimulated by intracellular cAMP

Representative trace displaying the effect of 10 μM forskolin together with 200 μM IBMX (FSK/IBMX; added as indicated by the arrow) on 3T3-L1 adipocyte membrane capacitance as well as histogram showing the average exocytotic rate ($\Delta C/\Delta t$). The trace is representative of 8 individual experiments.

Figure 5: The developed model can predict adiponectin release levels at different time points

A) Time-resolved predictions with uncertainties from simulations of the final model structure and the found acceptable parameters. In the simulated predictions, levels of cAMP, ATP and Ca^{2+} were varied to reflect the experimentally added FSK/IBMX (left), FSK/IBMX in cells pre-treated with BAPTA (middle) and a combination of FSK/IBMX and ionomycin (right). B) Summary of the predicted adiponectin release intervals at time point 30 minutes in A). C) Experimental data from (6) showing adiponectin release under the same conditions as simulated in B). D) Time-resolved predicted

adiponectin release after FSK/IBMX addition. E) Experimental adiponectin release at the indicated time-points (*cf.* simulations in D). Included concentrations were: 10 μM forskolin, 200 μM IBMX, and 1 μM ionomycin. Ca^{2+} -chelated cells were pre-treated with 50 μM BAPTA during 30 min. * $P < 0.05$; ** $P < 0.01$; *** $P < 0.001$,

Figure 6: Ca^{2+} -dependent endocytosis contributes to the capacitance measurements

A) Illustrative figure and equation showing how intervals of the endocytosis contribution to the measured capacitance signal were calculated. B) Calculated endocytosis contribution under indicated different intracellular condition (cAMP and ATP present at 100 μM and 3 mM respectively).

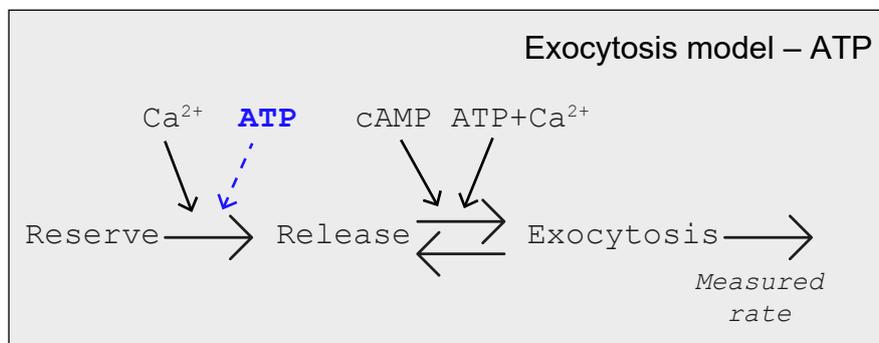
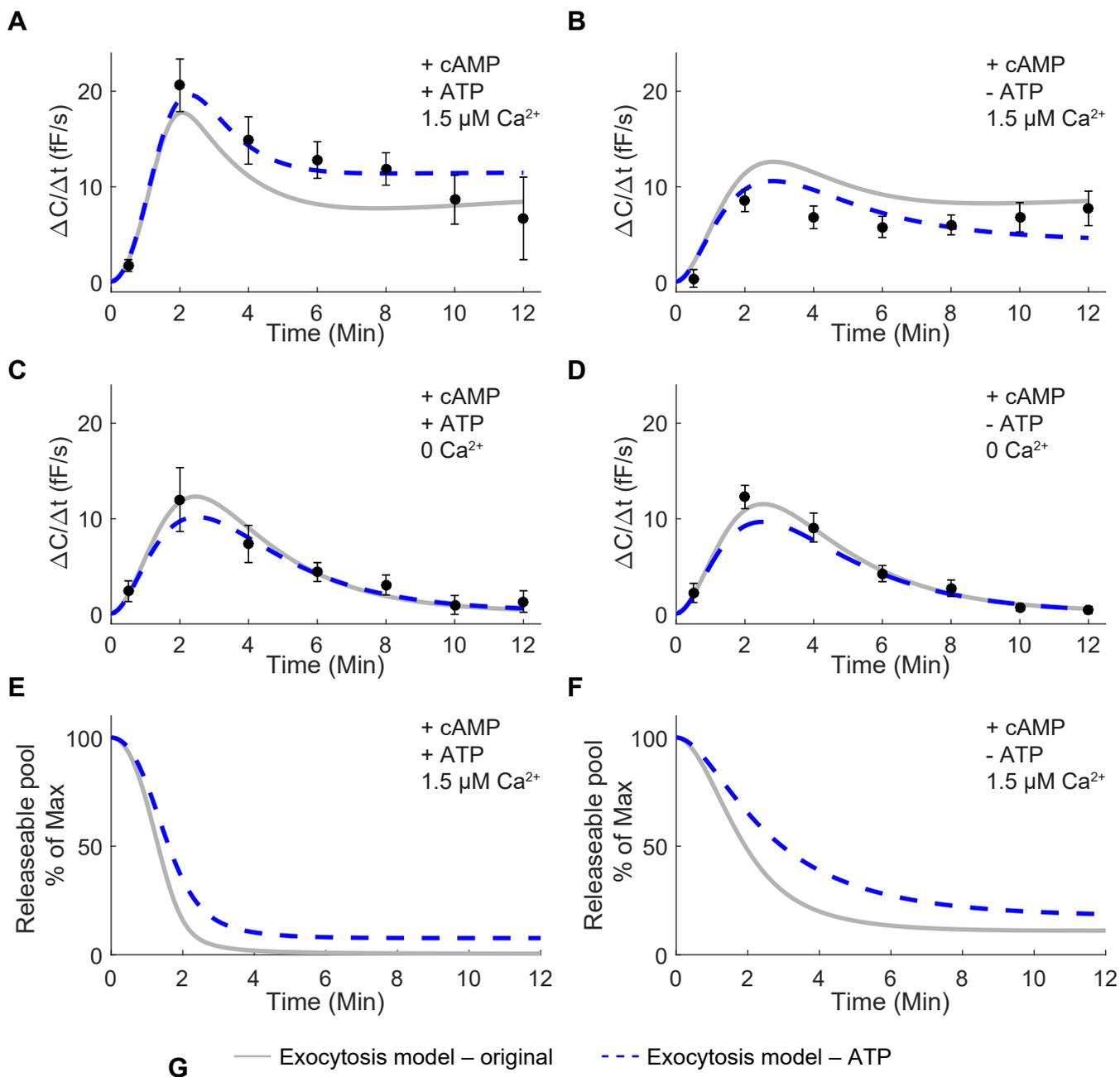
Figure 7: The final model including endocytosis and back-translation to interaction graph

The developed model with ATP/endocytosis included and back-translation to an interaction graph including the cell physiological insights from this work. In agreement with the original model (Fig. 1A) adiponectin exocytosis is triggered by cAMP alone and augmented by the combination of ATP and Ca^{2+} . As revealed by the present study, ATP- is also required in combination with Ca^{2+} in order for adiponectin containing vesicles to attain release competence (in our model, to be transferred from the reserve pool to the releasable pool). In addition to stimulating exocytosis, Ca^{2+} also induces membrane retrieval (endocytosis). The Ca^{2+} -triggered endocytosis needs to be preceded by cAMP-triggered exocytosis (*cf.* Fig 3C). The contribution of Ca^{2+} -dependent endocytosis to the measured signal is substantial at unphysiologically high intracellular Ca^{2+} concentrations (see text for more details).

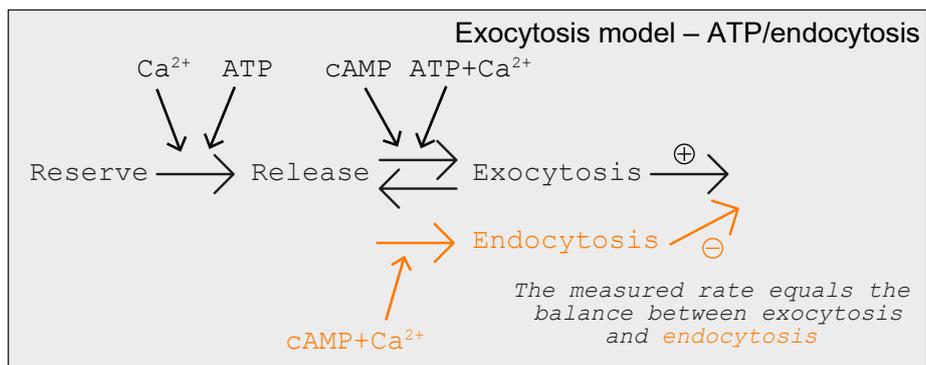
Figure 8: CARS and MPEF microscopy

Fully differentiated 3T3-L1 adipocytes imaged using CARS and MPEF. CARS signal in red and CellTracker™ Red shown in blue. Scale bar =50 μm .

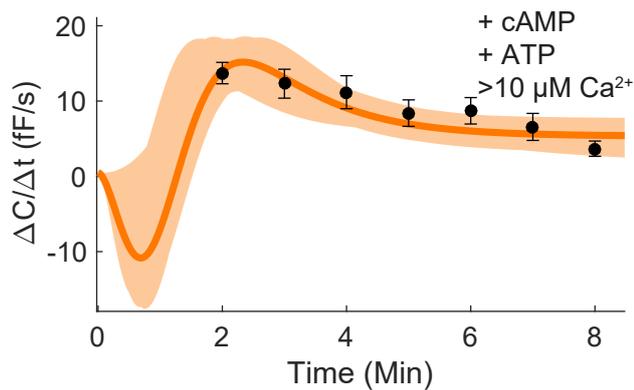
Figure 2



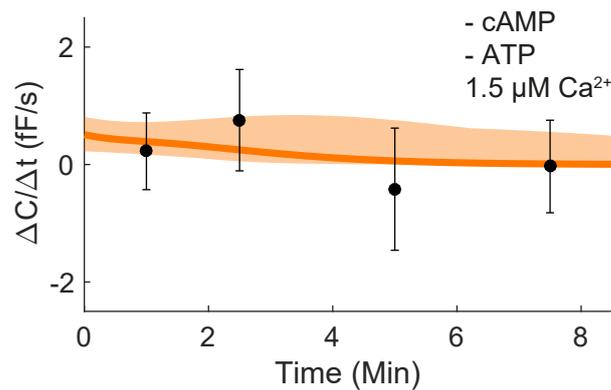
A



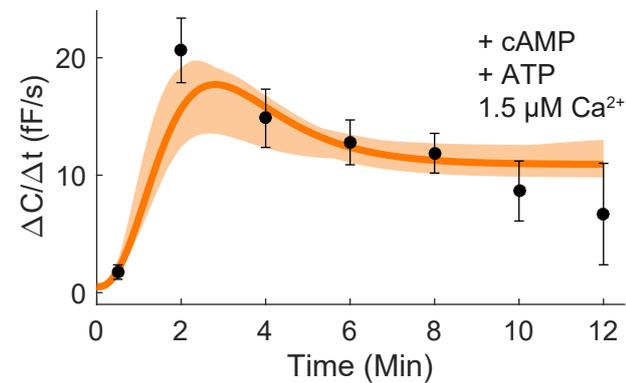
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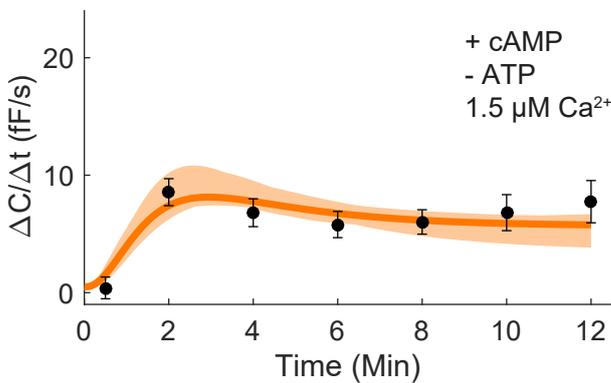
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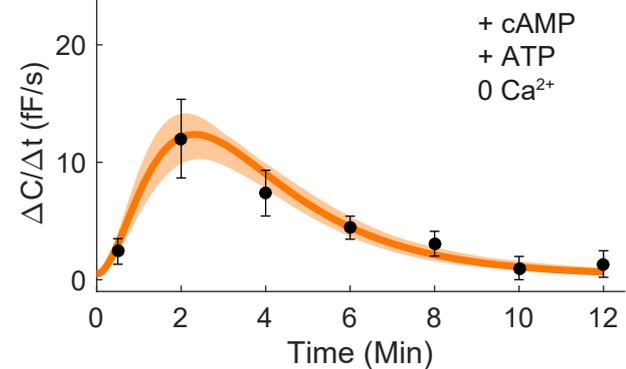
D



E



F



G

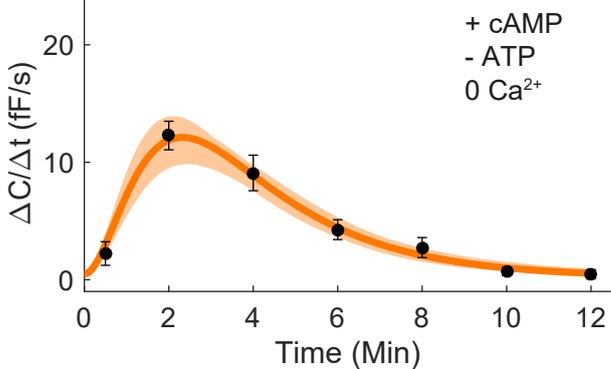


Figure 4

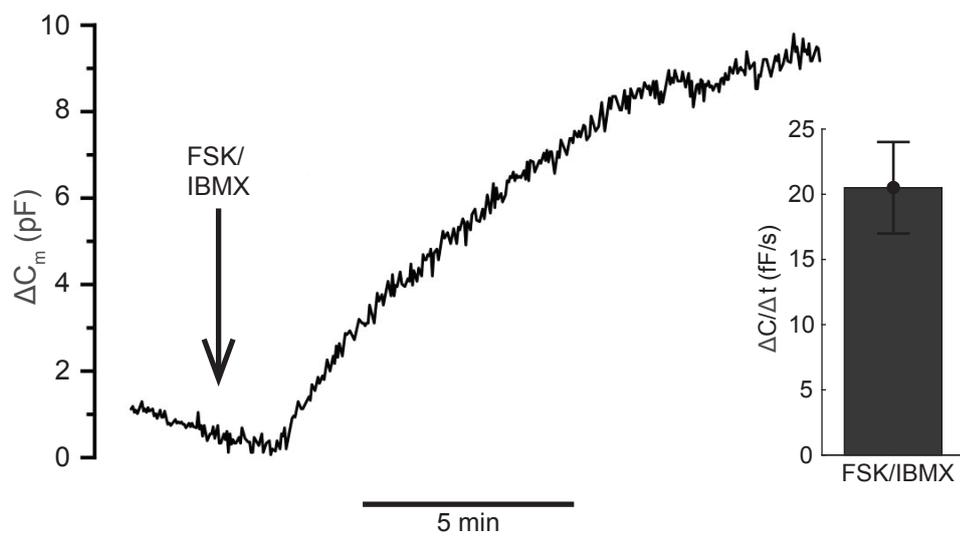
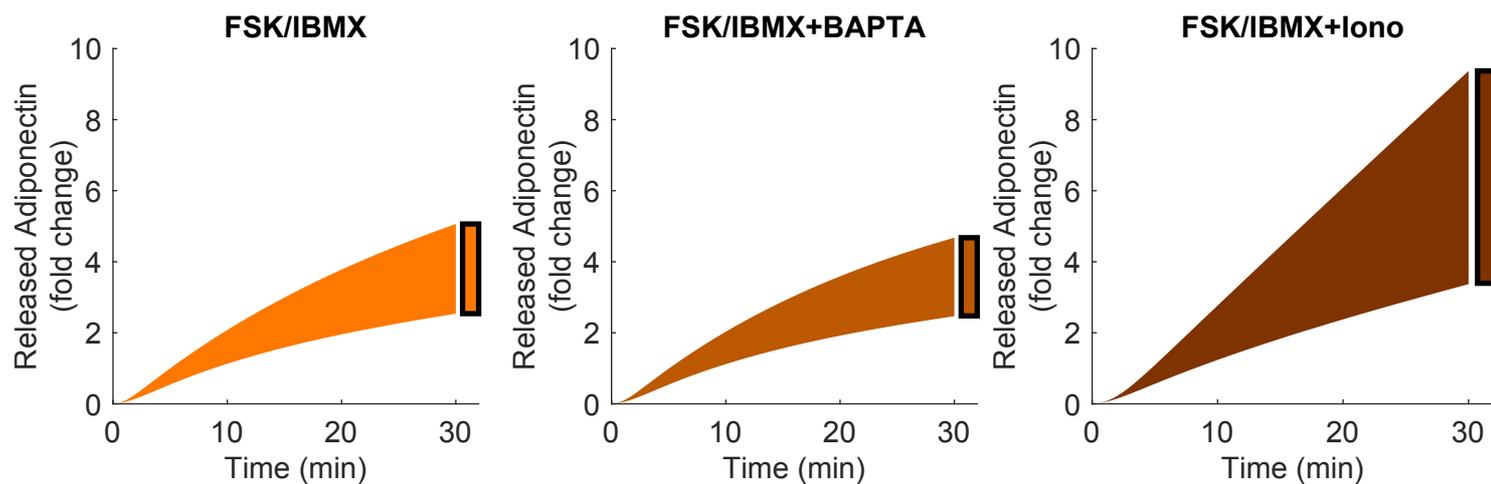


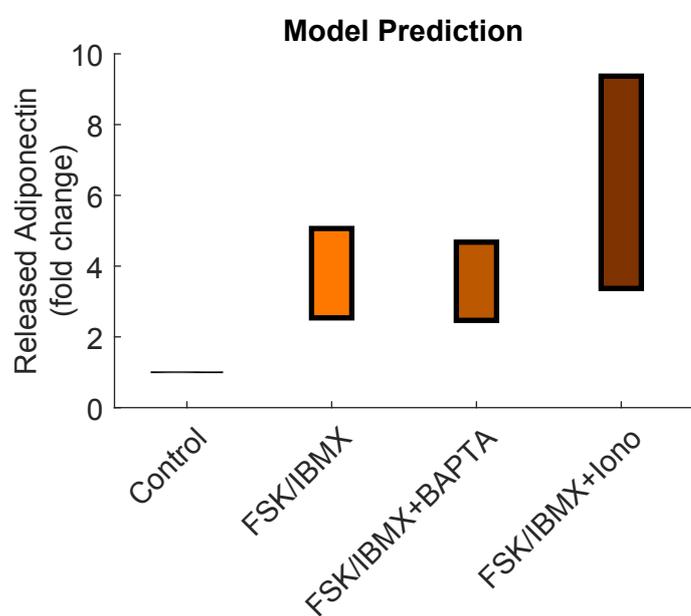
Figure 5

A

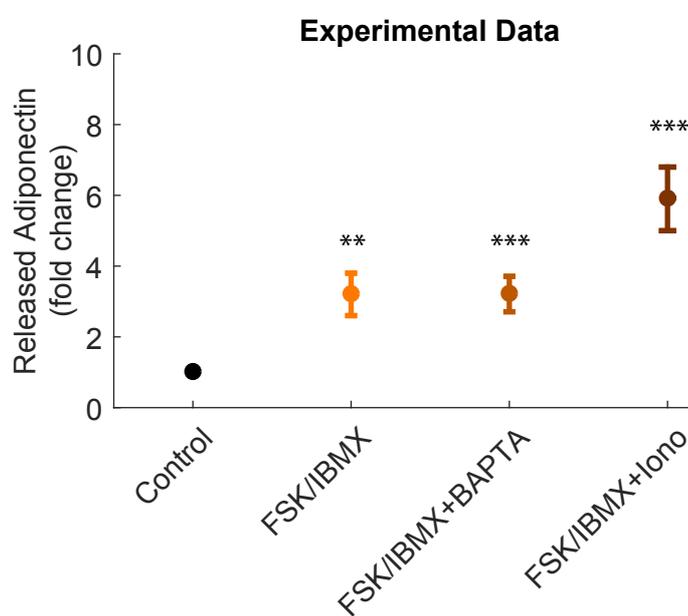
Model Predictions



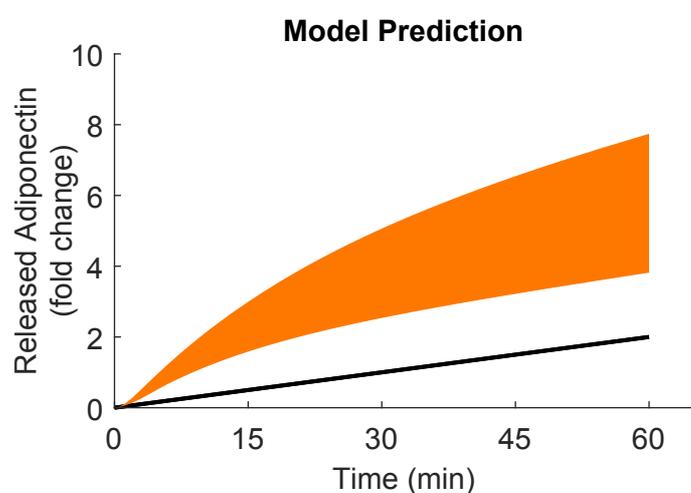
B



C



D



E

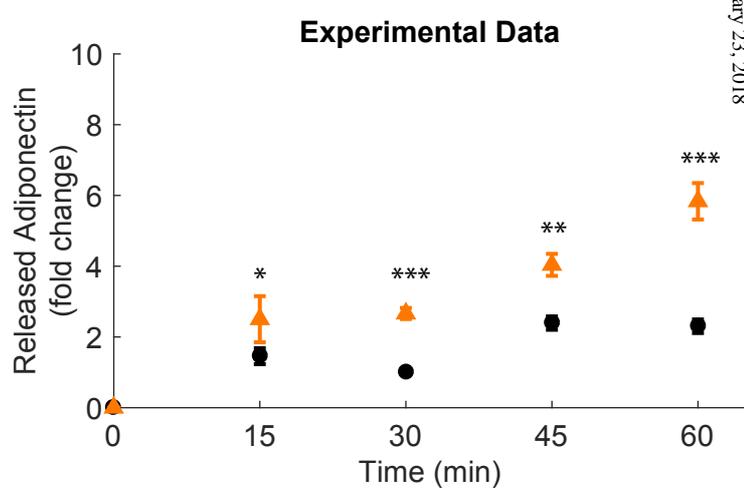
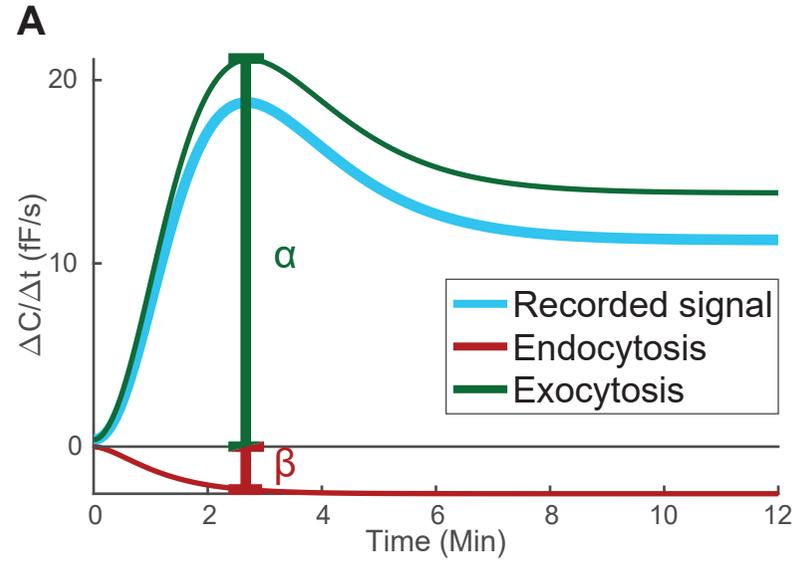
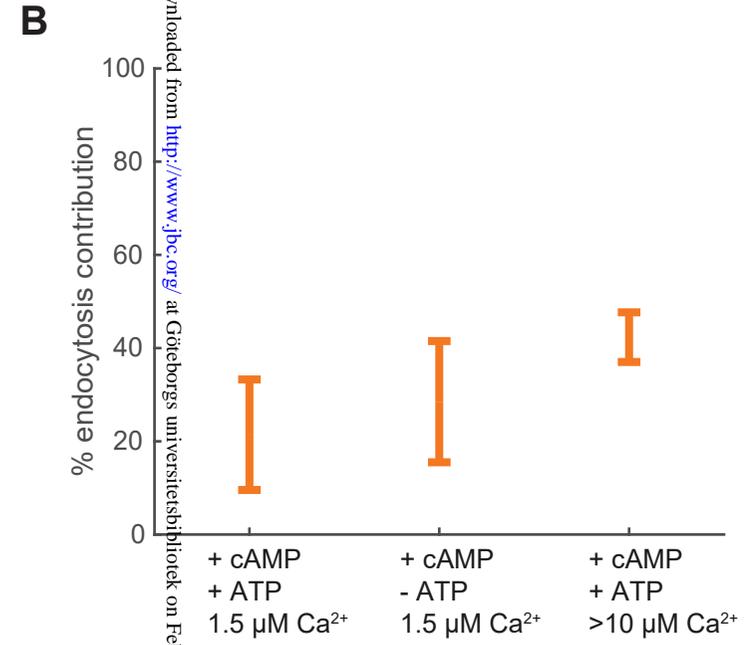
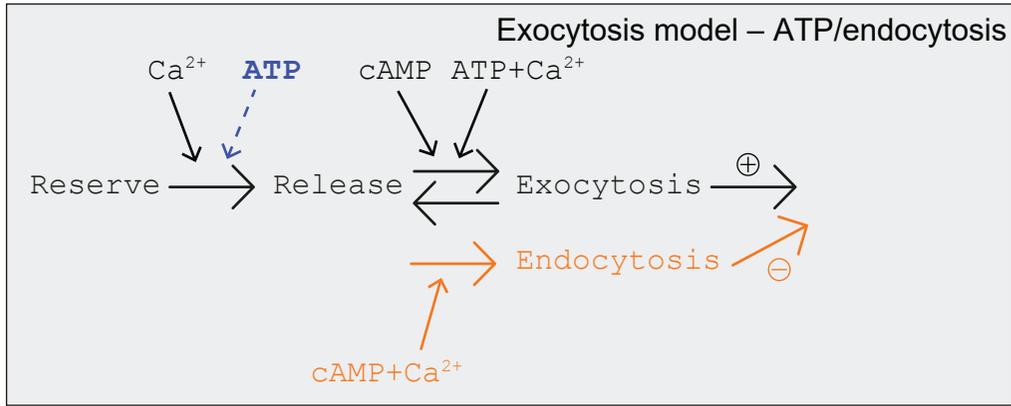


Figure 6



$$\% \text{ endocytosis} = \frac{|\beta|}{|\alpha| + |\beta|} \cdot 100$$





Back-translation

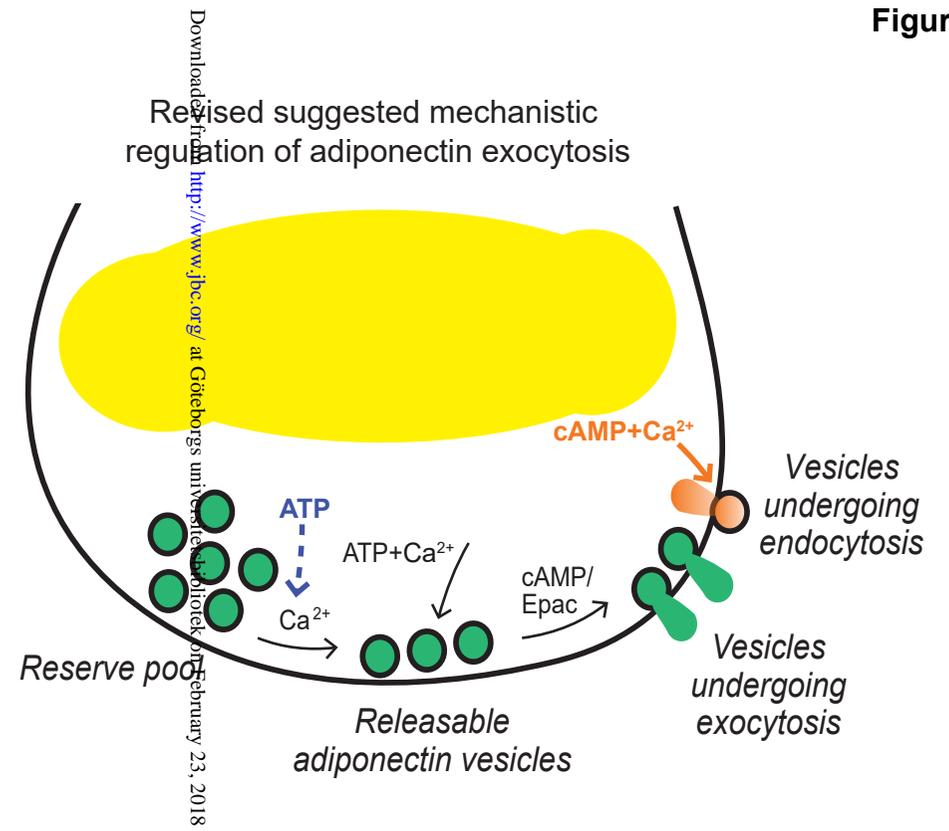
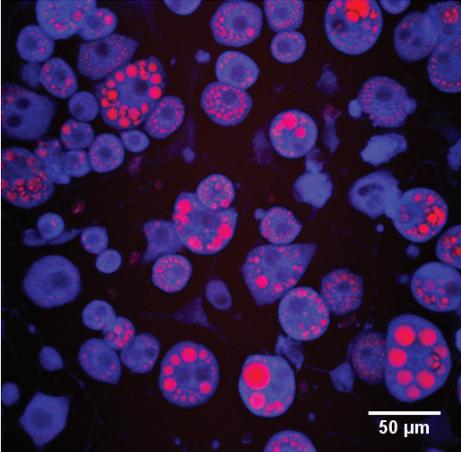


Figure 8



Mathematical modeling of white adipocyte exocytosis predicts adiponectin secretion and quantifies the rate of vesicle exo- and endocytosis.

Cecilia Brännmark, William Lövfors, Ali M. Komai, Tom Axelsson, Mickaël F. El Hachmane, Saliha Musovic, Alexandra Paul, Elin Nyman and Charlotta S. Olofsson

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